

# Shape Fluctuations of Microemulsion Droplets Studied by Neutron Spin Echo (NSE)

Dobrin P. Bossev,<sup>1</sup> Antonio Faraone<sup>2</sup>  
and Steven Kline<sup>2</sup>

<sup>1</sup>*Indiana University, Bloomington, IN 47405*

<sup>2</sup>*NIST, Center for Neutron Research  
Gaithersburg, MD 20899*

*Summer School on Methods and Applications of Neutron Spectroscopy  
June 20-24, 2005  
NIST Center for Neutron Research, Gaithersburg, MD 20899*

## Content

---

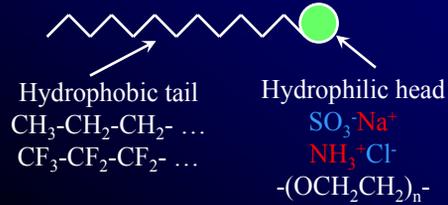
- **Surfactant aggregates in solution**
- **Why NSE?**
- **Experimental system**
- **Data analysis**

# Surfactants

Oils and water do not mix! Why?  
Water is a polar liquid,  $\epsilon = 81$   
Oils are non polar,  $\epsilon \sim 2$   
( $\epsilon$  - dielectric const.)

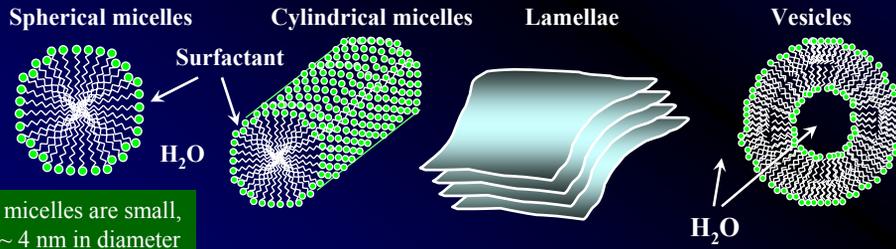
Surfactant = "Surface Active Agent"

Surfactant molecule: **two portions**



When surfactants are **dissolved in water**:

- reduce the surface tension because they are adsorbed on the surfaces
- form variety of aggregates – micelles, lamellae, bicelles, vesicles, etc



# Applications

**Surfactants are very useful to:**

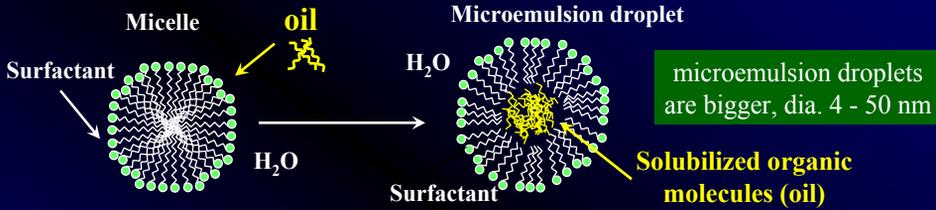
- Reduce the interfacial tension
- Solubilize oils in water
- Stabilize liquid films & foams
- Modify the interparticle interactions
- Stabilize dispersions
- Modify the contact angle & wetting
- ...

**Surfactants in our daily life:**

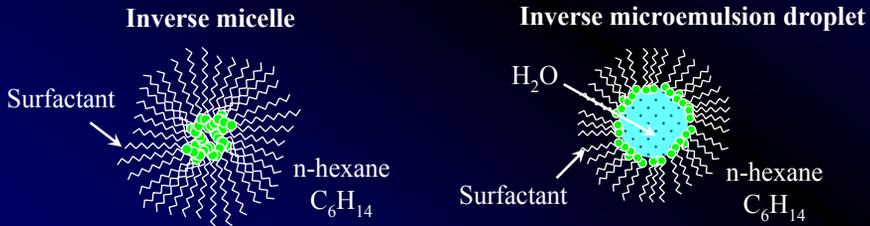
- Food – mayonnaise, margarine, ice cream, milk, ...
- Industry – lubricants, stabilizers, emulsifiers, foamers, detergents, ...
- Medicine – drugs, bio applications, (lungs), ...
- Cosmetics – moisturizers, lotions, healthcare products ...
- Agriculture – aerosols, fertilizers ...
- ...

# Micellar properties

Oils and water do not mix?!? The surfactants help them mix.

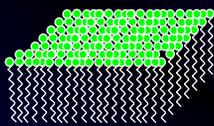


Surfactants form “inverse” micelles in oils:



# Properties of the surfactant film

## Surfactant film



### Parameters:

- Molecular structure
- Additives
- Ionic strength
- Co-surfactant
- Temperature, pressure etc.

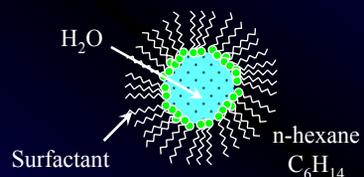
## Properties of the surfactant film:

- Interfacial tension  $\longleftrightarrow$
- Lateral elasticity  $\longleftrightarrow\longleftrightarrow$
- Spontaneous curvature
- Bending elasticity
- Saddle splay elasticity

$$E = \int \left[ \gamma + \frac{k}{2} \left( \frac{1}{R_1} + \frac{1}{R_2} - \frac{2}{R_s} \right) + \frac{\bar{k}}{R_1 R_2} \right] dS$$

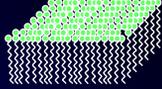
### Microemulsions:

- Thermodynamically stable, isotropic, and optically transparent solutions
- $R \sim 2 - 50$  nm (good scatterers)
- The curvature of the surfactant film can be controlled

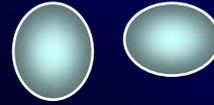
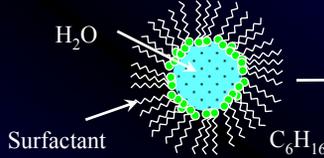


# How to measure bending elasticity

Surfactant film:  
bending elasticity



The surfactant film is a very soft material  
Bending elasticity  $\Rightarrow$  Thermal undulations  
(highly localized)



Shape fluctuations are in  
a very short time and  
length scales!

- SANS: static method
- NMR relaxation times: relaxation model?
- Dynamic light scattering: large  $T$  &  $L$  scales
- **NSE**:  $T$  scale  $\sim 0.01 - 100$  ns,  $L$  scale  $\sim 1 - 10$  nm

# Experimental

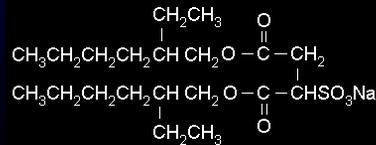
Shape fluctuations in **AOT/D<sub>2</sub>O/C<sub>6</sub>D<sub>14</sub>** microemulsion

Surfactant molecule:

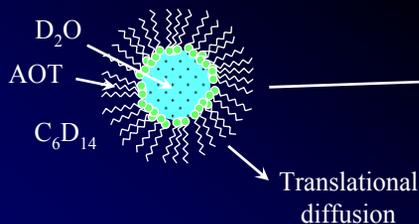


Hydrophobic tail    Hydrophilic head

**AOT**



Inverse microemulsion droplet



Shape fluctuations



# Shell contrast

cross section (barn)

H: 82.0    D: 7.6

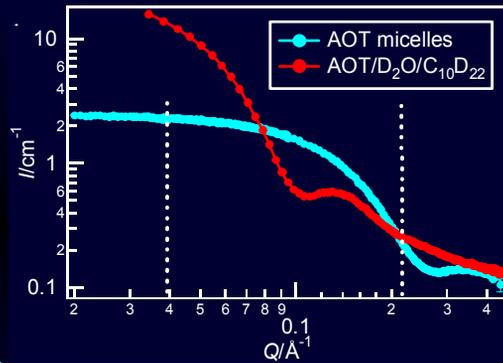
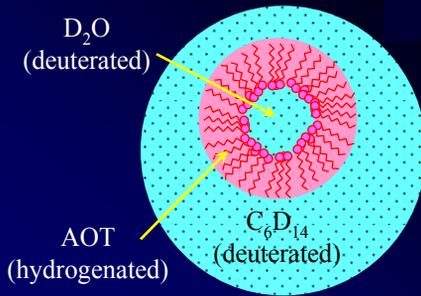
SLD ( $\times 10^{-6} \text{ \AA}^{-2}$ )

*n*-hexane -0.49

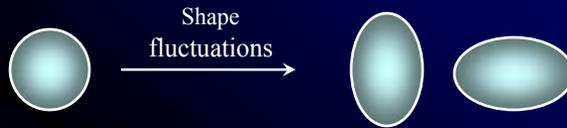
H<sub>2</sub>O -0.56

*d*-hexane 6.5

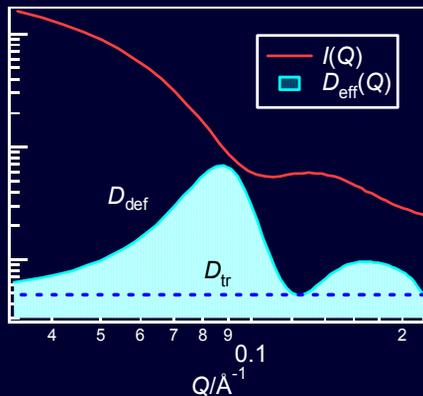
D<sub>2</sub>O 6.4



# Data analysis



$$E_{bend} = \frac{k}{2} \int dS \left( \frac{1}{R_1} + \frac{1}{R_2} - \frac{2}{R_s} \right) + \bar{k} \int dS \frac{1}{R_1 R_2}$$



Expansion of  $r$  in spherical harmonics with amplitude  $a$ :

$$r(\Omega) = r_0 \left( 1 + \sum_{l,m} a_{lm} Y_{lm}(\Omega) \right)$$

Frequency of oscillations of a droplet:

$$\lambda_2 = \frac{k}{\eta R_0^3} \left[ 4 \frac{R_0}{R_s} - 3 \frac{\bar{k}}{k} - \frac{3k_B T}{4\pi k} f(\phi) \right] \frac{24\eta}{23\eta' + 32\eta}$$

## Summary of data analysis

**Micelles:**  
translational diffusion  $\longrightarrow \frac{I(Q,t)}{I(Q,0)} = \exp[-D_{eff} Q^2 t]$

**Microemulsions:**  
translational diffusion + shape deformations  $\longrightarrow \frac{I(Q,t)}{I(Q,0)} = \exp[-D_{eff}(Q) Q^2 t]$

$$D_{eff}(Q) = D_{tr} + D_{def}(Q) \quad D_{eff}(Q) = D_{tr} + \frac{5\lambda_2 f_2(QR_0) \langle |a_2|^2 \rangle}{Q^2 [4\pi [j_0(QR_0)]^2 + 5f_2(QR_0) \langle |a_2|^2 \rangle]}$$

**Goal:** Bending modulus of elasticity

$$k = \frac{1}{48} \left[ \frac{k_B T}{\pi p^2} + \lambda_2 \eta R_0^3 \frac{23\eta' + 32\eta}{3\eta} \right]$$

$$f_2(QR_0) = 5[4j_2(QR_0) - QR_0 j_3(QR_0)]^2$$

$\lambda_2$  – the damping frequency – **frequency of deformation**

$\langle |a|^2 \rangle$  – mean square displacement of the 2-nd harmonic – **amplitude of deformation**

$p^2$  – size polydispersity, measurable by SANS or DLS

## Summary

- **NSE is a dynamic scattering method that yields the intermediate scattering function  $I(q,t)$ . NSE has the highest energy resolution among the neutron scattering methods, which is achieved by using the neutron precession in magnetic fields as an “internal” clock**

- **NSE is suitable for studies on soft condensed matter:**

- Brownian diffusion in micellar systems
- Shape fluctuations of lipid membranes and thin films
- Intra-molecular diffusion of proteins
- Local segmental diffusion of polymers in solution
- Intra- and inter- molecular dynamics of polymer melts and glasses
- Other thermal fluctuations of soft matter etc (time scale: 0.01 – 200 ns)

- **Some limitations:**

- The samples must produce strong scattering
- Hydrogenated samples in deuterated matrix are the best choice
- Samples must not be magnetic
- The scattering should be in appropriate Q-range ( $0.04 < Q < 1.7 \text{ \AA}^{-1}$ )